



# P2P VoD: Does it Scale?

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## Problem statement

- Fundamental idea in P2P: clients also act as servers
- P2P VoD: combines file sharing (video exists) and realtime streaming (user wants to view file asap)

- Fundamental question: Are P2P VoD systems scalable?

- (Qiu & Srikant, 2004) : P2P file sharing systems can scale independent of peer arrival rate if peers cooperate “even a little bit”
- (Parvez et al., 2008): similar conclusions for VoD using simplified playback phase modeling

- We give a fluid model where playback phase is modeled explicitly and characterize conditions for acceptable QoS.

## Fluid model (1)

– Assumptions:

- All users have same upload ( $\mu$ ) and download ( $c$ ) capacities
- Users leave once the video is over (conservative assumption)
- $z$  = time to watch video (video size / coding rate)

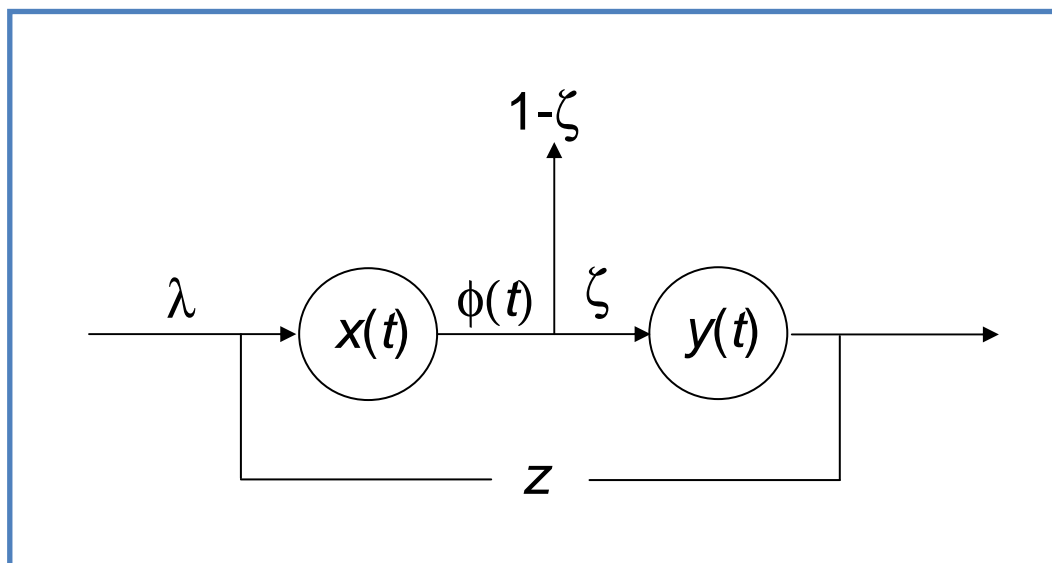
– Other parameters:

- $\eta$  = sharing efficiency factor (peer/chunk selection policies)
- $\zeta$  = probability that a leacher will stay as a seed
- $k$  = number permanent seeds (that never leave)

– State variables:

- $x(t)$  = number of leachers at time  $t$
- $y(t)$  = number of seeds at time  $t$

## Fluid model (2)

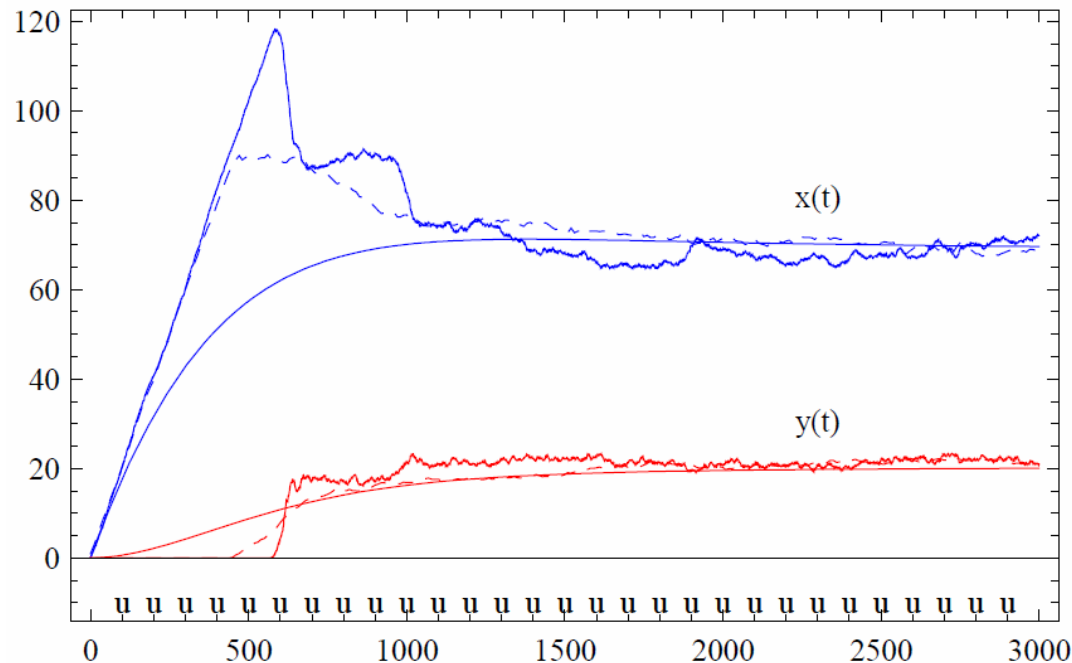


$$\begin{cases} x'(t) = \lambda - \phi(t), \\ y'(t) = \zeta\phi(t) - \frac{y(t)}{z - x(t)/\lambda} \end{cases}$$

$$\phi(t) = \min\{cx(t), \mu(\eta x(t) + y(t) + k)\}$$

## Validation

- Compare  $x(t)$ ,  $y(t)$  from fluid model (solid) with stochastic model (dashed) and BitTorrent simulations (jagged)



**Steady state is approximated very accurately!**

## Steady-state analysis

- Solve  $x'(t) = y'(t) = 0 \Rightarrow$  explicit steady-state solution  $(\bar{x}, \bar{y})$  for upload and download constrained cases
- Positivity, uniqueness, stability of  $(\bar{x}, \bar{y})$ 
  - $\bar{x} \geq 0, \bar{y} \geq 0, \phi(t)$  is satisfied at steady state
  - local stability of differential equations

## Steady-state synthesis

- The system has a unique and stable equilibrium and QoS is good (service rate > coding rate) if

$$\eta > \frac{1}{z} \left( \frac{1}{\mu} - \frac{k}{\lambda} \right)$$

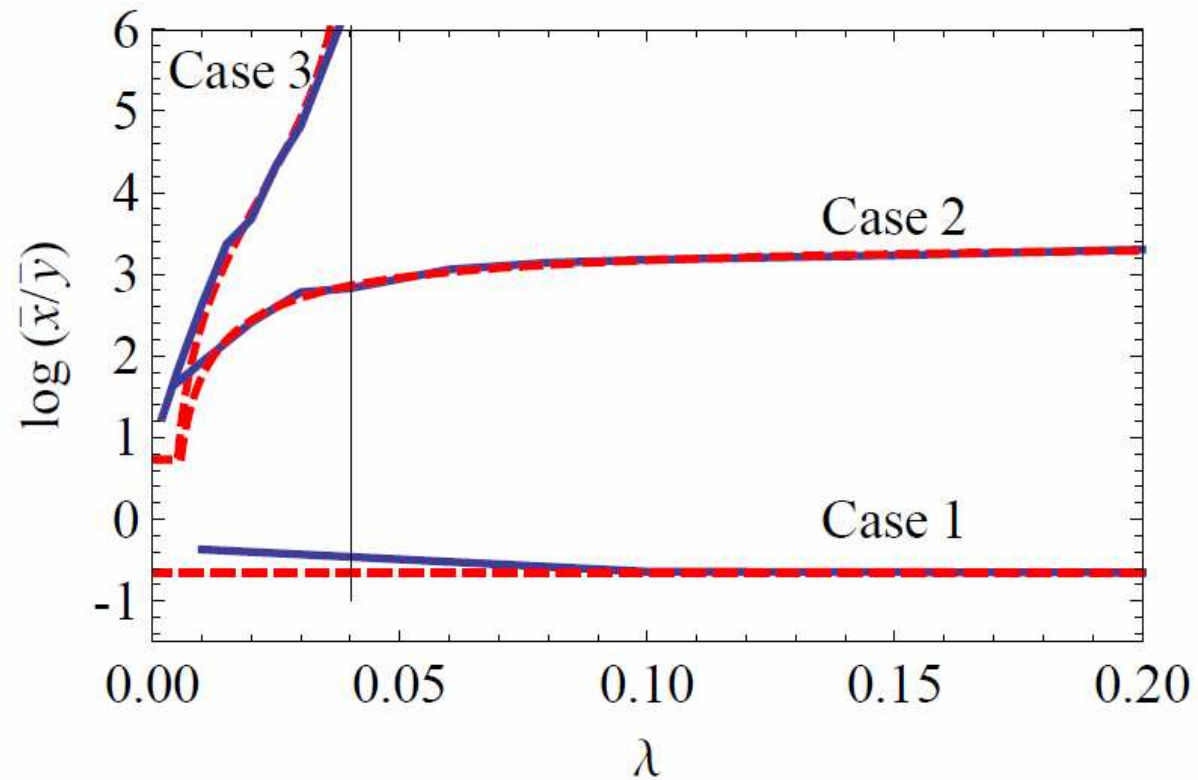
- System is scalable (QoS ok independent of arrival rate  $\lambda$ ) if

$$\eta > \frac{1}{z\mu}$$

- Scalability is independent of permanent seeds/altruism

**Efficiency  $\eta$  is critical for operation!**

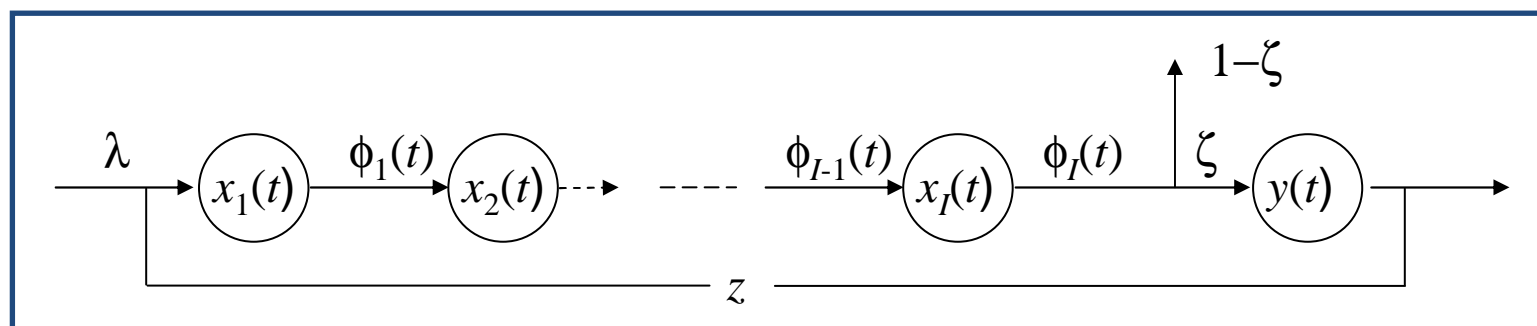
## Scalability example





## Fluid model for segmented system

- Efficiency parameter  $\eta$  not "very natural"
  - In VoD only older peers can help younger ones
  
- Segmented system without  $\eta$  parameter



- Exact analysis not possible...
- Segmented system is never scalable, but limit can be improved by increasing number of phases (last phase is the bottle neck)

## Conclusions

- Fluid models for analyzing P2P VoD
  - Black-box model, with  $h$  parameter
  - Segmented model
- Scalability
  - Black-box model: system can scale if efficiency is "good enough"
  - Segmented model: never scalable, but limit can be improved by splitting in smaller segments
- Open questions:
  - What happens in the limit when nof segments goes to infinity?
  - Impact of peer capacity heterogeneity?

## Papers

1. S. Aalto, P. Lassila, N. Raatikainen, P. Savolainen and S. Tarkoma, “P2P Video-on-Demand: Steady State and Scalability”, in *Proceedings of IEEE Globecom*, 2010.
2. S. Aalto, P. Lassila, S. Tarkoma and P. Savolainen, “Segmented P2P Video-on-Demand: Modeling and Performance”, in *Proceedings of 22nd International Teletraffic Congress (ITC 22)*, 2010.